University of Ljubljana, Faculty of Computer and Information Science

A brief revision of neural networks



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Contents

- a gentle introduction to neural networks
- feed forward neural networks
- backpropagation
- convolutional neural networks
- attacks on neural networks

read Chapter 7 in Jurafsky & Martin, 3rd edition,

Sources

- Richard Socher: *Deep Learning for Natural Language Processing*. Coursera
- Ian Goodfellow and Yoshua Bengio and Aaron Courville: *Deep Learning*. MIT Press, 2016, <u>http://www.deeplearningbook.org</u>
- Yoav Goldberg: A Primer on Neural Network Models for Natural Language Processing. *Journal of Artificial Intelligence Research* 57:345-420, 2016
- Keras library
- PyTorch

Artificial neural networks (ANN)

- universal function Approximator
- intuition: neurons

 in successive layers
 encode useful
 features



Artificial neural networks and brain analogy – a neuron



more than a hundred types of neurons in brain

Artificial neuron



Input

The brain analogy is far from realistic: a neuron cell is highly complex, and so are interconnections.

Perceptron



Inputs

Activation functions

• examples: step function, sigmoid (logistic)



Activation functions

- ReLU (rectified linear unit)
 f(x) = max(0, x)
- softplus / approximation of ReLU with continuous derivation
 f(x) = ln(1+e^x)
- many others



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Learning: error backpropagation

- a single neuron is weak
- a network of neurons can approximate any continuous function
- deep neural network: more than one hidden level



• learning: error backpropagation

Backpropagation learning algorithm for NN

- Backpropagation: A neural network learning algorithm
- Started by psychologists and neurobiologists to develop and test computational analogues of neurons
- A neural network: A set of connected input/output units where each connection has a weight associated with it
- During the learning phase, the network learns by adjusting the weights so as to be able to predict the correct class label of the input tuples
- Also referred to as connectionist learning due to the connections between units

A multi-layer feed-forward NN



How a multi-layer NN works?

- The inputs to the network correspond to the attributes measured for each training tuple
- Inputs are fed simultaneously into the units making up the input layer
- They are then weighted and fed simultaneously to a hidden layer
- The number of hidden layers is arbitrary; if more than 1 hidden layer is used, the network is called deep neural network
- The weighted outputs of the last hidden layer are input to units making up the **output layer**, which emits the network's prediction
- The network is **feed-forward**: None of the weights cycles back to an input unit or to an output unit of a previous layer
- If we have backwards connections the network is called recurrent neural network
- From a statistical point of view, networks perform **nonlinear regression**: Given enough hidden units and enough training samples, they can closely approximate any function



deep neural networks + large data sets + GPU (+many new ideas) **X**₁ **X**₂ **y**₁ **y**₂ Xn

Input

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Hidden layer(s)



Why nonlinear activation function?

- The product of two linear transformations is itself a linear transformation.
- What is a derivative of a sigmoid?



• Values are propagated from input through the network till the output layer which returns the prediction













Softmax

 normalizes the output scores to be a probability distribution (values between 0 and 1, the sum is 1)



Criterion function

 together with softmax we frequently use cross entropy as cost function C

$$C = -\sum_{j} t_{j} \log y_{j}$$

target value
$$\frac{\partial C}{\partial z_{i}} = \sum_{j} \frac{\partial C}{\partial y_{j}} \frac{\partial y_{j}}{\partial z_{i}} = y_{i} - t_{i}$$

Learning with error backpropagation

- Backpropagation
- randomly initialize parameters (weights)
- compute error on the output
- compute contributions to error, δ_n , on each step backwards $w'_{(x1)1} = w_{(x1)1} + \eta \delta_1 \frac{d}{d}$
- gradient
- step
- iteratively
- batch
- minibatch



- We will do gradient descent on the whole network.
- Training will proceed from the last layer to the first.



Next 18 slides by Andrew Rosenberg

Introduce variables over the neural network

$$\vec{\theta} = \{w_{ij}, w_{jk}, w_{kl}\}$$



Error Backpropagation $\vec{\theta} = \{w_{ij}, w_{jk}, w_{kl}\}$

- Introduce variables over the neural network
 - Distinguish the input and output of each node







 $\vec{\theta} = \{w_{ij}, w_{jk}, w_{kl}\}$

Training: Take the gradient of the last component and iterate backwards





$$L_{n} = \frac{1}{2} \left(y_{n} - f(x_{n}) \right)^{2}$$

$$\frac{\partial R}{\partial w_{kl}} = \frac{1}{N} \sum_{n} \left[\frac{\partial L_n}{\partial a_{l,n}} \right] \left[\frac{\partial a_{l,n}}{\partial w_{kl}} \right]$$
 Calculus chain rule



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$$\frac{\partial R}{\partial w_{kl}} = \frac{1}{N} \sum_{n} \left[\frac{\partial \frac{1}{2} (y_n - g(a_{l,n}))^2}{\partial a_{l,n}} \right] \left[\frac{\partial a_{l,n}}{\partial w_{kl}} \right]$$



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 $L_n = \frac{1}{2} \left(y_n - f(x_n) \right)^2$

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 $\frac{\partial R}{\partial w_{kl}} = \frac{1}{N} \sum_{n} \delta_{l,n} z_{k,n}$

Optimize last hidden weights w_{ik}

$$\frac{\partial R}{\partial w_{jk}} = \frac{1}{N} \sum_{n} \left[\frac{\partial L_n}{\partial a_{k,n}} \right] \left[\frac{\partial a_{k,n}}{\partial w_{jk}} \right]$$

$$x_{0}$$

$$x_{1}$$

$$x_{P}$$

$$x_{P}$$

$$x_{1}$$

$$x_{P}$$

$$x_{1}$$

$$x_{P}$$

$$x_{1}$$

$$x_{2}$$

$$x_{P}$$

$$x_{1}$$

$$x_{2}$$

$$x_{P}$$

$$x_{1}$$

$$x_{2}$$

$$x_{P}$$

$$x_{P$$

 $\frac{\partial R}{\partial w_{l,l}} = \frac{1}{N} \sum \delta_{l,n} z_{k,n}$

Optimize last hidden weights w_{ik}

$$\frac{\partial R}{\partial w_{jk}} = \frac{1}{N} \sum_{n} \left[\sum_{l} \frac{\partial L_{n}}{\partial a_{l,n}} \frac{\partial a_{l,n}}{\partial a_{k,n}} \right] \left[\frac{\partial a_{k,n}}{\partial w_{jk}} \right]$$
 Multivariate chain rule













Repeat for all previous layers

$$\frac{\partial R}{\partial w_{kl}} = \frac{1}{N} \sum_{n} \left[\frac{\partial L_{n}}{\partial a_{l,n}} \right] \left[\frac{\partial a_{l,n}}{\partial w_{kl}} \right] = \frac{1}{N} \sum_{n} \left[-(y_{n} - z_{l,n})g'(a_{l,n}) \right] z_{k,n} = \frac{1}{N} \sum_{n} \delta_{l,n} z_{k,n}$$

$$\frac{\partial R}{\partial w_{jk}} = \frac{1}{N} \sum_{n} \left[\frac{\partial L_{n}}{\partial a_{k,n}} \right] \left[\frac{\partial a_{k,n}}{\partial w_{jk}} \right] = \frac{1}{N} \sum_{n} \left[\sum_{l} \delta_{l,n} w_{kl} g'(a_{k,n}) \right] z_{j,n} = \frac{1}{N} \sum_{n} \delta_{k,n} z_{j,n}$$

$$\frac{\partial R}{\partial w_{ij}} = \frac{1}{N} \sum_{n} \left[\frac{\partial L_{n}}{\partial a_{j,n}} \right] \left[\frac{\partial a_{j,n}}{\partial w_{ij}} \right] = \frac{1}{N} \sum_{n} \left[\sum_{k} \delta_{k,n} w_{jk} g'(a_{j,n}) \right] z_{i,n} = \frac{1}{N} \sum_{n} \delta_{j,n} z_{i,n}$$

$$\frac{z_{i}}{w_{ij}} \int_{w_{ij}} \frac{z_{j}}{w_{jk}} \int_{w_{jk}} \frac{a_{k}}{w_{kl}} \int_{w_{kl}} \frac{z_{l}}{w_{kl}} \int_{w_{kl}} f(x, \vec{\theta})$$

$$x_{0}$$

$$x_{1}$$

$$x_{0}$$

$$x_{1}$$

$$x_{1}$$

$$x_{1}$$

$$x_{2}$$

$$x_{1}$$

$$x_{2}$$

$$x_{2}$$

$$x_{2}$$

$$x_{3}$$

$$x_{4}$$

$$x_{4}$$

$$x_{4}$$

Now that we have well defined gradients for each parameter, update using Gradient Descent





- Error backpropagation unravels the multivariate chain rule and solves the gradient for each partial component separately.
- The target values for each layer come from the next layer.
- This feeds the errors back along the network.



Backpropagation algorithm

- Iteratively process a set of training tuples & compare the network's prediction with the actual known target value
- For each training tuple, the weights are modified to **minimize the mean squared error** between the network's prediction and the actual target value
- Modifications are made in the "backwards" direction: from the output layer, through each hidden layer down to the first hidden layer, hence "backpropagation"
- Steps
 - Initialize weights to small random numbers, associated with biases
 - Propagate the inputs forward (by applying activation function)
 - Backpropagate the error (by updating weights and biases)
 - Terminating condition (when error is very small, etc.)

Defining a network topology

- Decide the network topology: Specify # of units in the *input* layer, # of hidden layers (if > 1), # of units in each hidden layer, and # of units in the *output layer*
- Normalize the input values for each attribute measured in the training tuples to [0.0—1.0]
- One input unit per domain value, each initialized to 0
- Output, if for classification and more than two classes, one output unit per class is used
- Once a network has been trained and its accuracy is unacceptable, repeat the training process with a *different network topology* or a *different set of initial weights*

Neural network as a classifier

- Weakness
 - Long training time
 - Require a number of parameters typically best determined empirically, e.g., the network topology or "structure."
 - Poor interpretability: difficult to interpret the symbolic meaning behind the learned weights and of "hidden units" in the network
- Strength
 - High tolerance to noisy data
 - Ability to classify untrained patterns
 - Well-suited for continuous-valued inputs and outputs
 - Successful on an array of real-world data, e.g., hand-written letters
 - Algorithms are inherently parallel
 - Techniques exist for the extraction of explanations from trained neural networks

Efficiency and interpretability

- Efficiency of backpropagation: Each epoch (one iteration through the training set) takes O(|D| * w), with |D| tuples and w weights, but # of epochs can be exponential to n, the number of inputs, in worst case
- For easier comprehension: Rule extraction by network pruning
 - Simplify the network structure by removing weighted links that have the least effect on the trained network
 - Then perform link, unit, or activation value clustering
 - The set of input and activation values are studied to derive rules describing the relationship between the input and hidden unit layers
- Sensitivity analysis: assess the impact that a given input variable has on a network output. The knowledge gained from this analysis can be represented in rules

Interpretation of hidden yayers

- What are the hidden layers doing?!
- Feature Extraction
- The non-linearities in the feature extraction can make interpretation of the hidden layers very difficult.
- This leads to Neural Networks being treated as black boxes.

Deep learning = learning of hierarchical representation



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

Overfitting and model complexity

- which curve is more plausible given the data?
- overfitting
- neural nets are especially prone to overfitting
- why?



Approaches to prevent overfitting

- Weight-decay
- Weight-sharing
- Early stopping
- Model averaging
- Bayesian fitting of neural nets
- Dropout
- Generative pre-training
- etc.

Deep learning successes

ILSVRC top-5 error rate on ImageNet





Microsoft claims new speech recognition record, achieving a super-human 5.1% error rate



Weaknesses of deep learning



Failures on out of-distribution examples

Michael A. Alcorn, Qi Li, Zhitao Gong, Chengfei Wang, Long Mai, Wei-Shinn Ku, Anh Nguyen (2018): Strike (with) a Pose: Neural Networks

Are Easily Fooled by Strange Poses of Familiar Objects. arXiv:1811.11553



school bus 1.0 garbage truck 0.99 punching bag 1.0 snowplow 0.92



motor scooter 0.99 parachute 1.0

.0 bobs

bobsled 1.0

parachute 0.54



fire truck 0.99

school bus 0.98

fireboat 0.98



Attacks on neural networks





What follows: more neural networks

- neural language models and word2vec representation
- convolutional neural networks
- recurrent neural networks for text and ELMo representation
- transformer networks and BERT representation
- middle level of language technologies (mostly based on neural nets): morphosyntactical analysis, dependency parsing, word sense disambiguation, semantic role labelling
- higher level of language technologies (mostly based on neural nets): machine translation, summarization, questions & answers, emotional computing